

Probability - GRADE 10

Exercises - A

Exercise A

QUESTION 8

8.1 At a certain school there are 64 boys in Grade 10. Their sport preferences are indicated below:

- 24 boys play soccer ✓
- 28 boys play rugby ✓
- 10 boys play both soccer and rugby ✓
- 22 boys do not play soccer or rugby ✓

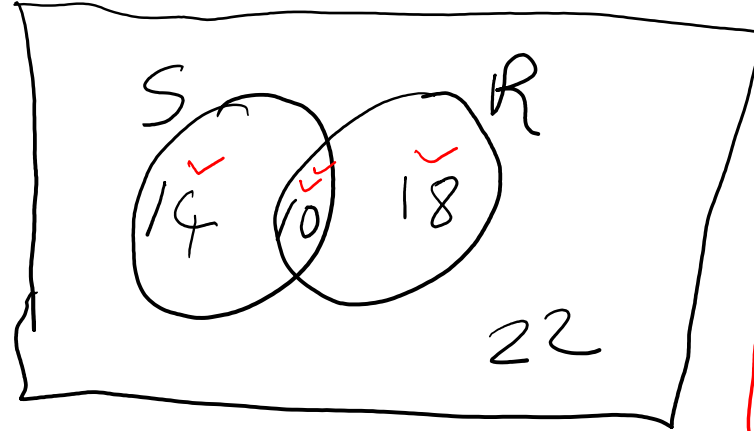
- 8.1.1 Represent the information above in a Venn diagram.
- 8.1.2 Calculate the probability that a Grade 10 boy at the school, selected at random, plays:
- Soccer and rugby
 - Soccer or rugby
- 8.1.3 Are the events a Grade 10 boy plays soccer at the school and a Grade 10 boy plays rugby at the school, mutually exclusive? Justify your answer.

Identity:

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

Solutions

8.1.1



Sample Space

8.1.2(b)

$$\frac{14 + 10 + 18}{64} = 0,66$$

8.1.2 (a) $\frac{10}{64} = 0,16$

$$\begin{aligned} \text{(b) } P(S \text{ or } R) &= P(S) + P(R) - P(S \text{ and } R) \\ &= \frac{24}{64} + \frac{28}{64} - 0,16 \\ &= 0,66 \end{aligned}$$

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Mutually exclusive
 $P(A \text{ and } B) = 0$

$$8.1.3 \quad P(S \text{ and } R) = 0,16$$

$$\therefore P(S \text{ and } R) \neq 0$$

\therefore No, the events are not mutually exclusive.

Probability - GRADE 10

Exercises - A

Exercise A

- 8.2 One morning Samuel conducted a survey in his residential area to establish how many passengers, excluding the driver, travel in a car. The results are shown in the table below:

Number of passengers, excluding the driver	0	1	2	3	4
Number of cars	7	11	6	5	1

Calculate the probability that, excluding the driver, there are more than two passengers in a car.

- 8.3 If you throw two dice at the same time, the probability that a six will be shown on one of the dice is $\frac{10}{36}$ and the probability that a six will be shown on both the dice, is $\frac{1}{36}$. What is the probability that a six will NOT show on either of the dice when you throw two dice at the same time?

$$8.2 \text{ Sample space} = 7 + 11 + 6 + 5 + 1 \\ = 30$$

$$\therefore \frac{5}{30} + \frac{1}{30} = \frac{1}{5} = 0,2$$

$$8.3 \quad 1 - P(\text{Six Show})$$

$$= 1 - \left(\frac{10}{36} + \frac{1}{36} \right)$$

$$= \frac{25}{36}$$

$$= 0,69$$

Probability - GRADE 10

Exercises - B

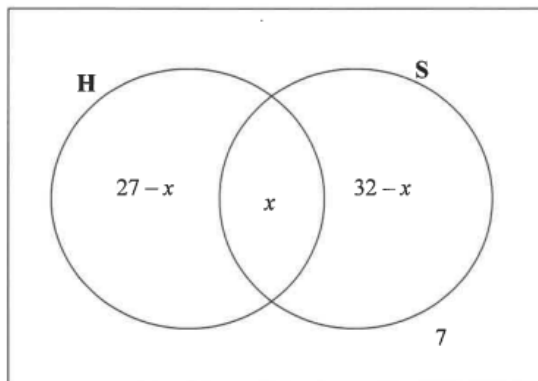
Exercise B

QUESTION 8

8.1 In a certain class of 42 boys:

- 27 play hockey (H)
- 32 play soccer (S)
- 7 do not play hockey or soccer
- An unknown number (x) play both hockey and soccer

The information is represented in the Venn diagram below.



8.1.1 Calculate the value of x .

8.1.2 If a boy from the class is chosen at random, calculate the probability that he:

- Does not play hockey or soccer
- Plays only soccer

Solutions

$$8.1.1 \quad 27 - x + x + 32 - x + 7 = 42$$

$$66 - x = 42$$

$$66 - 42 = x$$

$$24 = x$$

$$\therefore x = 24$$

$$8.1.2 \text{ (a)} \quad \frac{7}{42} = 0,17$$

$$\text{(b)} \quad \frac{32 - 24}{42} = 0,19$$

Probability - GRADE 10

Exercises - B

Exercise B

8.2 A bag contains 3 blue balls and x yellow balls.

8.2.1 Write down the total number of balls in the bag.

8.2.2 If a ball is drawn from the bag, write down the probability that it is blue.

8.3 8.3.1 Complete the following statement:

If A and B are two mutually exclusive events, then
 $P(A \text{ and } B) = \dots$

8.3.2 Given that A and B are mutually exclusive events. The probability that event A occurs is 0,55. The probability that event B does not occur is 0,7.

Calculate $P(A \text{ or } B)$.

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$P(A \text{ or } B) = P(A) + P(B) - 0$$

$$8.2.1 \quad x + 3$$

$$8.2.2 \quad \frac{3}{(x + 3)}$$

$$8.3.1 \quad P(A \text{ and } B) = 0$$

$$8.3.2 \quad P(\text{not } B) = 0,7$$

$$\begin{aligned} P(B) &= 1 - P(\text{not } B) \\ &= 1 - 0,7 \\ &= 0,3 \end{aligned}$$

$$\begin{aligned} \therefore P(A \text{ or } B) &= P(A) + P(B) - 0 \\ &= 0,55 + 0,3 = 0,85 \end{aligned}$$

A and B
are mutually
exclusive
 $\therefore P(A \text{ and } B) = 0$

Probability - GRADE 10

Exercises - C

Exercise C

QUESTION 7

7.1 Two events, A and B, are complementary and make up the entire sample space. Also, $P(A') = 0,35$.

7.1.1 Complete the statement: $P(A) + P(B) = \dots$

7.1.2 Write down the value of $P(A \text{ and } B)$.

7.1.3 Write down the value of $P(B)$.

7.2 A survey was conducted among 150 learners in Grade 10 at a certain school to establish how many of them owned the following devices: smartphone (S) or tablet (T).

The results were as follows:

- 8 learners did not own either a smartphone or a tablet.
- 20 learners owned both a smartphone and a tablet.
- 48 learners owned a tablet.
- x learners owned a smartphone.

7.2.1 Represent the information above in a Venn diagram.

7.2.2 How many learners owned only a smartphone?

7.2.3 Calculate the probability that a learner selected at random from this group:

- Owned only a smartphone
- Owned at most one type of device

Solutions,

$$7.1.1 P(A) + P(B) = 1$$

$$7.1.2 P(A \text{ and } B) = 0$$

$$7.1.3 B \text{ is } A'$$

$$P(B) = P(A') \\ = 0,35$$

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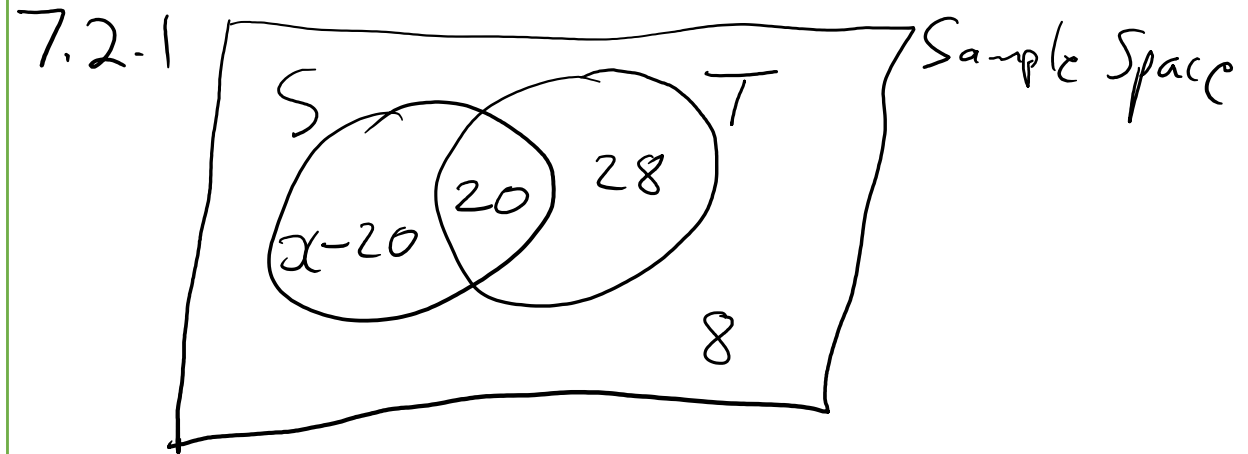
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$$7.2.2 \quad x - 20 + 20 + 28 + 8 = 150$$
$$x = 114$$

$$\therefore \text{only}(S) = 114 - 20 = 94$$

$$7.2.3 \text{ (a)} \quad \frac{94}{150} = 0,63$$

$$\text{(b)} \quad \frac{94}{150} + \frac{28}{150} + \frac{8}{150} = 0,87$$